#### **Summary Slide for Experiments**



## **Inferential Statistics**

 go beyond the actual data in hand...
 ...and make a "best guess" about the population from which the sample was taken



can be wrong ... even when you do everything right

## **Inferential Statistics**

- Step Zero: get the descriptive stats (mean & sd)
- Step One: get a best guess for whatever you're interested in

e.g., the difference between two means get an estimate of how wrong you might be

Step Two (optional; "hypothesis testing"): convert the values from Step One into a yes-or-no answer

e.g., are the means for these conditions different in the entire sampling population ... yes or no?

- 1a) best guess for population mean
  = sample mean
- 1b) estimate for how wrong you might be
  = sample standard deviation divided by √N
  this is called the "standard error (of the mean)"

Note: standard error has an associated value to indicate how wrong it might be (etc, etc)

this is the "degrees of freedom" = N-1

 note: there is no "validity" associated with Step One because we haven't made an inference yet

 to make an inferential statement about the mean, you must make some assumptions
 the most important assumption concerns the shape of the distribution of means





sample mean ( $\overline{X}$ )

how do you express a point estimation?

old-fashioned: you calculate the "window" or interval that has a 95% chance of including the population value

new standard: just provide the best guess and the estimate of how wrong you could be; i.e.,  $\overline{X}$  & se

# **Design Types**

- assume an experiment with two conditions (i.e., the smallest possible experiment)
- there are two ways that you can run this all subjects participate in both conditions within-subjects design different groups of subjects in each condition between-subjects design
- this is a huge decision; today you'll start to see why

## Paired-samples t-test

- Step Two (yes-or-no answer)
- when you use a within-subjects design, you get pairs of data ... Condition 1 and Condition 2
   when what you're interested in is whether there is a difference between conditions – yes or no – you convert each pair to a difference score, and ask the yes-or-no question:

*is the mean <u>difference</u> something other than zero?* new question: how different from zero must the sample mean be in order for you to say *yes*?

### Paired-samples t-test

frequency



sample mean difference  $(\overline{D})$ 

where is zero in this plot?

what is the probability of getting the observed mean difference, assuming this distribution?

rule in psychology: if the probability of getting what we found is less than 5%, then we say that the pop mean is not zero

## Some More Standard Symbols

- μ (mu): population mean [unknown ... usual target]
- X (X-bar): sample mean
- $\hat{\mu}$  (mu-hat): best guess for population mean =  $\overline{X}$
- sd (use full name): standard deviation in the sample
- se (use full name): standard error of the mean = sd/ $\sqrt{N}$
- df (use full name): degrees of freedom
- α (alpha): "significance" cut-off = .05 in psychology

## Independent-samples t-test

- Step Two (yes-or-no answer)
- when you use a between-subjects design, you have separate samples for Condition 1 and Condition 2
   so, the probability question (that leads to a "Yes" conclusion when the p-value is less than 5%) becomes:
  - what is the probability of getting two sample means that are this far apart if we assume both samples came from one distribution?

#### Independent-samples t-test





## what could go wrong?

- the answer depends on what you concluded
- if you concluded that a difference exists (in the pop) then you might be making a "false-alarm" error which is a Type-I error

 if you concluded that there isn't a difference then you might be making a "miss" error ... Type-II

## All of the Standard Symbols

- μ (mu): population mean [unknown ... usual target]
- X (X-bar): sample mean
- $\hat{\mu}$  (mu-hat): best guess for population mean =  $\overline{X}$
- sd (use full name): standard deviation
- se (use full name): standard error of the mean = sd/ $\sqrt{N}$
- df (use full name): degrees of freedom
- α (alpha): "significance" cut-off = .05 in psychology
- 1-β (one minus beta): "power"; aim for .80+ in psych

## Inferential Errors (from t-tests)

what causes Type-I errors?

what causes Type-II errors?

what are the (main) assumptions?

## **Power and Design-type**

- what could go wrong and assumptions are the same as for both types of design
- the main difference between the two types of *t*-test (from a statistical point of view) is the size of β
   independent-samples *t*-tests have much less power (i.e., higher β) for a given number of subject